

Here is a interactive coordinate geometry program for the HP-41CX I wrote sometime in the 1980s.

	LBL "CGX"	PROMPT	RCL 04	-	FIX 4	LBL 08	LBL D
	RCLPTA	FC?C22	-	X<>Y	XEQ 08	2	SF 07
	LBL e	GTD 12	SIN	RCL 01	GETX	*	"OC PT?"
5	CLX	GTD 50	/	-	FC? 00	SEEKPT	PROMPT
	SEEKPT	LBL 11	GTD 50	R-P	STD 01	RTN	XEQ 40
	X<>F	"D1?"	LBL 13	STD 10	GETX	LBL 06	SF 00
	SF 27	PROMPT	"D2(-SH)?"	FS?C 01	FC?C 00	"DP?"	LBL E
	SF 21	FC?C 22	PROMPT	RTN	STD 02	PROMPT	"PIAP?"
	DEG	GTD 20	STD 06	X<>Y	"N="	STD 08	PROMPT
10	"EALN RSL"	STD 05	X<0?	360	ARCL Y	SF 01	E3
	PROMPT	"D2(-CC)?"	SF 06	MOD	AVIEW	SF 02	/
	LBL A	PROMPT	XEQ 06	STD 09	"E="	GTD 20	+
	"PTANPE?"	STD 06	RCL 03	"#"	ARCL X	LBL 90	STD 07
	PROMPT	X<0?	STD T	FIX 0	AVIEW	"POC?"	SF 07
15	X<>Z	SF 06	ST-Z	ARCL 00	ADV	PROMPT	LBL 07
	STD 07	XEQ 06	RDN	"T-"	FS? 07	STD 07	RCL 07
	SF 04	X?2	P-R	ARCL 07	RTN	CF 22	FS? 00
	GTD 80	RCL 05	X<>Y	AVIEW	FC? 05	"L?"	XEQ 20
20	LBL 6	X?2	X?2	COS	GTD e	PROMPT	FC? 00
	FC?C 00	+	RCL 06	"N"	FS? 00	HR	XEQ 40
	SF 00	RCL 06	X?2	X<0?	GTD 00	FS?C 22	1SG 07
	LBL B	X?2	X<>Y	"S"	FS?C 03	GTD 14	GTD 07
	FS? 05	-	-	RCL 09	GTD 90	"L?"	GTD e
	GTD 10	2	SQRT	SIN	FC?C 02	PROMPT	END
25	"ST PT?"	/	FS?C 06	X?0?	GTD B	RCL 10	
	PROMPT	RCL 05	CHS	"FE"	RCL 08	/	
	SF 05	/	+	X<=0?	STD 07	R-D	
	CF 00	RCL 10	LBL 50	"FW"	GTD 20	LBL 14	
	GTD 40	/	P-R	ASIN	LBL 00	STD Y	
30	LBL 10	ACOS	X<>Y	ABS	CF 02	RCL 09	324
	CF 22	FC?C 06	RCL 02	FS? 09	CF 03	180	steps
	"#"	CHS	+	"AZ="	GTD B	+	596
	FIX 0	+	X<>Y	FS? 09	LBL 09	+	bytes
	ARCL 00	RCL 05	RCL 01	RCL 09	X<>Y	STD 04	
35	"T-?"	GTD 50	+	HMS	HR	RDN	
	FIX 4	LBL 12	RCL 07	FIX 4	GTD IND Y	HMS	
	PROMPT	"B2?"	LBL 80	ARCL X	LBL 04	"Δ="	
	FC?C 22	PROMPT	XEQ 08	AVIEW	180	ARCL X	
40	GTD e	FC?C 22	RDN	"D="	-	AVIEW	
	X<0?	GTD 13	SAVEX	ARCL 10	LBL 02	LAST X	
	SF 03	XEQ 09	RDN	AVIEW	CHS	D-R	
	ABS	STD 04	SAVEX	ADV	LBL 03	RCL 10	
	STD 07	XEQ 06	RCL 07	RCL 07	180	*	
	"B1?"	X<>Y	FS?C 04	LBL 40	+	"L="	
45	PROMPT	RCL 04	GTD 40	FC? 00	LBL 01	ARCL X	
	FC?C 22	-	LBL 20	STD 00	CF 09	AVIEW	
	GTD 11	SIN	XEQ 08	"#"	RTN	ADV	
	XEQ 09	*	GETX	FIX 0	LBL 05	RCL 04	
	STD 03	RCL 03	GETX	ARCL X	SF 09	RCL 10	
50	"D1?"	STD 2	RCL 02	AVIEW	RTN	GTD 50	

To run, *type in data file name in Alpha register, then press
XEQ **ALPHA** **CGX** **ALPHA**

* Number of pts you can store is $\frac{1}{2} \times$ length of file
(e.g. a file sized with 50 regs holds 25 pts.)
Pt. numbering starts at 0 (zero).

Menu

EA	LN	RS	LS
A	B	D	E

EA \Rightarrow enter & assign
LN \Rightarrow lines
RS \Rightarrow radial stakeout
LS \Rightarrow list

Entering Bearings: Type in Bearing **ENTER**
Quad **R/S**

Quad codes are

1	=	NE
2	=	SE
3	=	SW
4	=	NW
5	=	NA

(Once an azimuth has been entered, the computer will always display azimuths until a bearing is entered, and vice-versa)

Sideshots: Press **B** to toggle between "sideshot" & "normal" mode. You are in sideshot mode when the little "0" is on the display.

- 1) when you exit the lines routine, SS mode is turned off.
- 2) when you restart at a new point, SS mode is turned off.
- 3) In sideshot mode, curves are not computed.
- 4) when you execute a radial stakeout, SS mode is turned on.
- 5) You may sideshot intersections.

Curves: To traverse curves, enter the radius point as a negative number. (Notice the little "3" comes on). Traverse or inverse to the radius point, enter the P.D.C. then give either the Δ or length. (If the curve turns left, Δ and L are negative values.)

Errors: If you make a serious mistake, or see a message like "DATA ERROR", press **E** to reset the computer and return to the menu.

Abbreviations:

ST	PT	starting point	NE	northeast	N	northing
B1		bearing 1	NW	northwest	E	easting
B2		bearing 2	SE	southeast	Δ	delta
D1		distance 1	SW	southwest	L	length
D2		distance 2	AZ	azimuth	OC PT	occupied point
CC		counterclockwise	D	distance	DP	destination point
SH		short	PT	point		

Registers

- 00 Current Pt #
- 01 Current N
- 02 Current E
- 03 Brg 1
- 04 Brg 2
- 05 Dist 1
- 06 Dist 2
- 07 Next Pt #
- 08 Dest Pt #
- 09 Ref Az
- 10 Ref Dist

Flags

- 00 Sideshot
- 01 Intersection Leg 1
- 02 Intersection Leg 2
- 03 Curve
- 04 List or Stakeout loop
- 05 Lines Routine
- 06 Short B-D or CC D-D
- 07 -
- 08 -
- 09 Display Azimuth
- 21 Printer on
- 22 Numeric entry
- 27 User mode

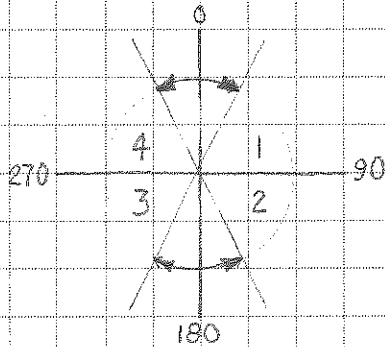
Keyboard

- A Enter & Assign
- B Lines
- D Radial Stakeout
- E List
- b Sideshot/Normal mode toggle
- e Error Reset

Local Labels

- 10 Lines Routine
- 11 B1 unknown
- 12 B1 known, D1 unknown
- 13 B1 known, D1 unknown, B2 unknown
- 50 Traverse
- 80 Store
- 20 Inverse
- 40 Display
- 09 Compute Azimuth
- 04 Q = NW
- 02 Q = SE
- 03 Q = SW
- 01 Q = NE
- 05 Q = NA
- 08 Set Data Pointer
- 06 Intersection Setup
- 90 Curve
- 14 Radial Brg out
- 07 List / Stakeout loop

Formulas



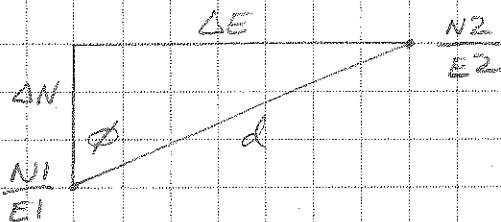
Brg \rightarrow Az :

Q1 : $Az = Brg$
 Q2 : $Az = 180 - Brg$
 Q3 : $Az = 180 + Brg$
 Q4 : $Az = 360 - Brg$

Az \rightarrow Brg : $Brg = |\sin^{-1}(\sin Az)|$

Quadrant code :	North	$\cos(Az) = +$	} NE $\cos +, \sin +$	
	South	$\cos(Az) = -$		SE $\cos -, \sin +$
	West	$\sin(Az) = -$		SW $\cos -, \sin -$
	East	$\sin(Az) = +$		NW $\cos +, \sin -$

Traverse, Inverse



$\phi =$ Azimuth from 1 to 2

$\Delta N = d \cos \phi$
 $\Delta E = d \sin \phi$
 $d = \sqrt{\Delta N^2 + \Delta E^2}$
 $\tan \phi = \Delta E / \Delta N$

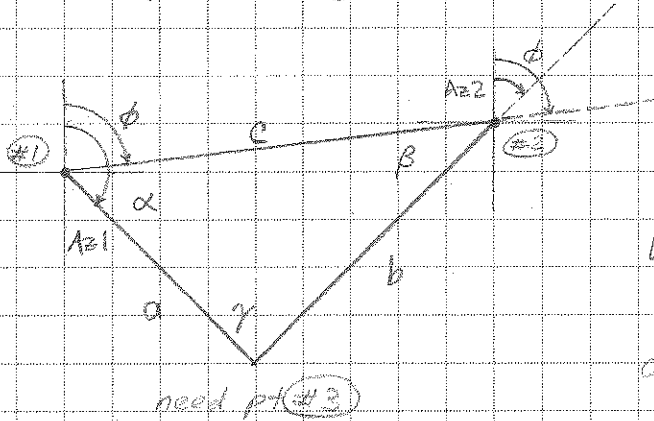
Use NP-41 **P-R** and **R-P** functions



Traverse : $N2 = N1 + \Delta N$
 $E2 = E1 + \Delta E$

Inverse : $\Delta N = N2 - N1$
 $\Delta E = E2 - E1$

Bearing-Bearing:



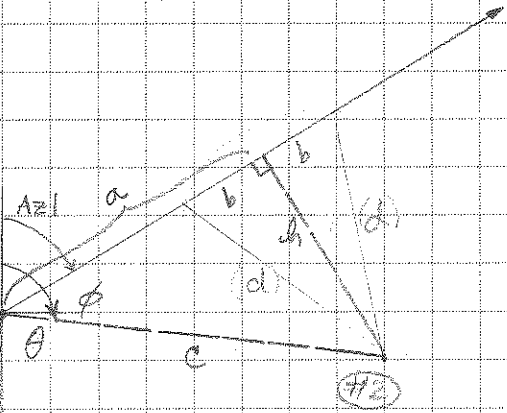
$\phi = \text{ref Az}$ $c = \text{ref dist.}$
 $\alpha = \text{Az1} - \phi$
 $\beta = \phi - \text{Az2}$
 $\gamma = 180 - \alpha + \beta$

Law of sines: $\frac{a}{\sin \beta} = \frac{c}{\sin \gamma}$
 $a = \frac{c \sin \beta}{\sin \gamma}$

since $\sin(180 - \theta) = \sin \theta$
 $a = \frac{c \sin \beta}{\sin(\alpha + \beta)} = \frac{c \sin(\phi - \text{Az2})}{\sin(\text{Az1} - \phi + \phi - \text{Az2})}$
 $= \frac{c \sin(\phi - \text{Az2})}{\sin(\text{Az1} - \text{Az2})}$

Note: You can specify Brg1 & Brg2
 "forward" or "backward" since
 $\sin(180 - \theta) = \sin \theta$

Bearing-Distance:



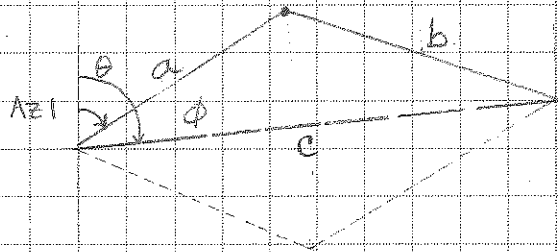
$\theta = \text{ref Az}$ $c = \text{ref dist}$
 $d = \text{known second distance}$
 $\phi = \theta - \text{Az1}$

$a = c \cos \phi$
 $h = c \sin \phi$
 $b = \sqrt{d^2 - h^2}$

for long solution use $a + b$ (CF 06)
 " short " " $a - b$ (SF 06)

Note: ϕ can be specified as either $\theta - \text{Az1}$ or $\text{Az1} - \theta$ since
 the sign of ϕ is unimportant
 since $a = c \cos \phi = c \cos(-\phi)$
 and $h^2 = (c \sin \phi)^2 = (-c \sin(-\phi))^2$
 Also, the sign of d is unimportant since
 it is only used as $d^2 = -d^2$

Distance - Distance:



θ = ref azimuth c = ref distance
 a = known first distance
 b = known second distance

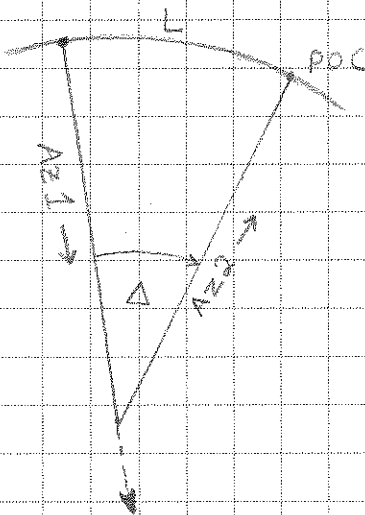
Law of cosines:

$$b^2 = a^2 + c^2 - 2ac \cos \phi$$

$$\phi = \cos^{-1} \left(\frac{a^2 + c^2 - b^2}{2ac} \right)$$

for clockwise soln (CF 06) use $AZ1 = \theta - \phi$
 " counterclockwise " (SF 06) " $AZ1 = \phi - \theta$

Curves:



$$AZ2 = \Delta + (AZ1 + 180)$$

$$L = \Delta_{rad} \cdot r$$

$$\Delta_{rad} = \frac{L}{r}$$

For curves turning to the left
 Δ or L is specified as a negative
 value

This is a sketch I used during development of the program

